

## Hand-In Assignment 2

1. Calculate  $3/7$  in base 3. [10 pts]

2. Let  $A = \{a, b, c\}$ . Define  $F : A \rightarrow P(A)$  by

$$F(x) = \begin{cases} \{a, b\} & \text{if } x = a \\ \{a, c\} & \text{if } x = b \\ \{b\} & \text{if } x = c \end{cases}$$

Compute  $S_F = \{x \in A; x \notin F(x)\}$  [10 pts]

3. Let  $A$  be a proper infinite subset of some set  $X$ . If  $x, y$  are two distinct elements of  $X$  that are not in  $A$ , we may set  $B = \{x, y\} \cup A$ . What is the cardinality of  $B$  in terms of the cardinality of  $A$ ? Justify your answer.

[10 pts]

4. Find a transfinite number that represents the cardinality of the open interval  $(0, 1)$  in terms of  $\aleph_0$ . Justify your answer. [10 pts]