

## Hand-In Assignment 3

1. Show that  $\mathbb{N}$  and  $\mathbb{Z}$  are homeomorphic under the usual metric by exhibiting a homeomorphism. [10 pts]
2. Prove that  $A$  is totally bounded if and only if every sequence  $\{x_n\}$  in  $A$  has a subsequence  $\{x_{n_k}\}$  for which  $d(x_{n_k}, x_{n_{k+1}}) < 2^{-k}$ . [10 pts]