

Directions: Each quiz should be completed in 20 minutes. Use the answer key to assign yourself a score. Please grade yourselves harshly.

Quiz 1

1. Evaluate $\lim_{x \rightarrow 2} \frac{x^{10} - 2^{10}}{x^5 - 2^5}$ [10 pts]

2. The position of a particle is given by $p(t) = t^2$. Calculate the velocity of the particle at $t = 1$. [10 pts]

3. Suppose that $f(x)$ is a bounded function that satisfies

$$1 \leq f(x) \leq 5$$

Calculate $\lim_{x \rightarrow 0} x^2 f(x)$ [10 pts]

Quiz 2

1. Compute $\lim_{x \rightarrow -\infty} \frac{\sqrt{5x^2 - 2}}{x + 3}$ [10 pts]

2. Let $f(x) = \frac{x^4 - 1}{x - 1}$. For which x is $f(x)$ discontinuous? Is the discontinuity(s) removable or not? [10 pts]

3. Suppose $\lim_{x \rightarrow \infty} f(x) = 5$, what is $\lim_{x \rightarrow 0^+} f\left(\frac{1}{x}\right)$? [10 pts]

Quiz 3

1. Let $f: [0, 1] \rightarrow (0, 1)$ be continuous. Show that for some $x \in [0, 1]$ $f(x) = x^2$
[10 pts]
2. Prove using a $\delta - \varepsilon$ argument that $\lim_{x \rightarrow -3} (2x + 1) = -5$ [10 pts]
3. Prove using a $\delta - \varepsilon$ argument that $\lim_{x \rightarrow 1} (x^2 - 2x) = -1$ [10 pts]

Quiz 4

1. Let $f(x) = \begin{cases} x^2 \sin\left(\frac{1}{x}\right) & \text{if } x \neq 0 \\ 0 & \text{if } x = 0 \end{cases}$

- (a) Determine whether $f'(0)$ exists. [5 pts]
 - (b) Is f continuous at $x = 0$? How do you know? [5 pts]
2. (a) Let $f(x) = x^{1/5}$. Use the definition of the derivative to compute $f'(x)$. [5 pts]
 - (b) For what x is f differentiable? [5 pts]
3. Let $f(x) = 2x^3 - x + 7$. Find the equation of the tangent line at the point $x = 1$.
[10 pts]
 4. Does the equation $\sqrt[3]{x} = 1 - x$ have a solution in $(0, 1)$? Justify your answer
[10 pts]